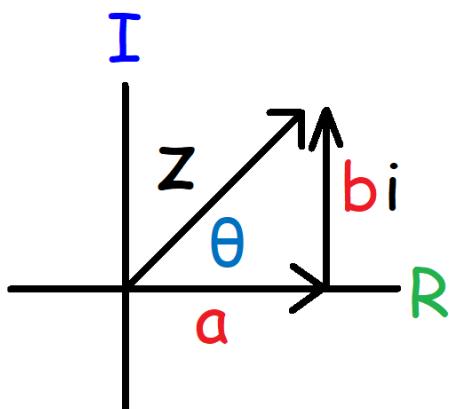


# Complex Numbers – Formula Sheet:

## Complex Numbers in Rectangular Form:



## Imaginary Numbers:

$$i = \sqrt{-1} \quad i^2 = -1 \quad i^3 = -i \quad i^4 = 1$$

## Complex Number in Rectangular Form:

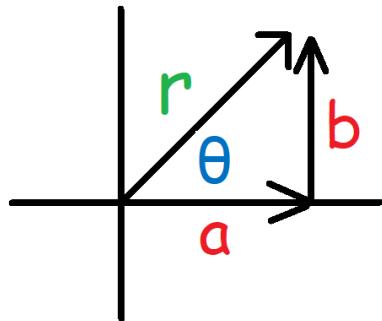
$$z = a + bi$$

$$a = r \cos \theta \quad b = r \sin \theta$$

## Absolute Value:

$$|z| = \sqrt{a^2 + b^2}$$

## Complex Numbers in Polar Form:



## Complex Numbers in Polar Form:

$$\begin{aligned} z_1 &= r_1[\cos \theta_1 + i \sin \theta_1] \\ z_2 &= r_2[\cos \theta_2 + i \sin \theta_2] \end{aligned}$$

## Modulus ( $r$ ) and Argument ( $θ$ ):

$$r = \sqrt{a^2 + b^2}$$

$$\theta = \tan^{-1}\left(\frac{b}{a}\right)$$

## Product of Two Complex Numbers:

$$z_1 \cdot z_2 = r_1 r_2 [\cos(\theta_1 + \theta_2) + i \sin(\theta_1 + \theta_2)]$$

## Quotient of Two Complex Numbers:

$$\frac{z_1}{z_2} = \frac{r_1}{r_2} [\cos(\theta_1 - \theta_2) + i \sin(\theta_1 - \theta_2)]$$

## De Moivre's Theorem – Power of Complex Number:

$$z^n = r^n [\cos(n\theta) + i \sin(n\theta)]$$

## De Moivre's Theorem – Roots of Complex Number:

$$z_k = \sqrt[n]{r} \left[ \cos\left(\frac{\theta + 2\pi k}{n}\right) + i \sin\left(\frac{\theta + 2\pi k}{n}\right) \right]$$

## Exponential to Polar Form:

$$e^{i\theta} = \cos \theta + i \sin \theta$$

$$z_k = \sqrt[n]{r} \left[ \cos\left(\frac{\theta + 360^\circ k}{n}\right) + i \sin\left(\frac{\theta + 360^\circ k}{n}\right) \right]$$

$$e^{i(0^\circ)} = 1$$

$$e^{i(90^\circ)} = i$$

$$k = 0, 1, 2, 3, 4, \dots n - 1$$

$$e^{i(180^\circ)} = -1$$

$$e^{i(270^\circ)} = -i$$

## Shortcut Notation:

$$r \text{ cis } \theta = r[\cos \theta + i \sin \theta]$$