

## Calculus 1 – Derivatives Formula Sheet:

<b>Basic Derivatives:</b>	$\frac{d}{dx}[c] = 0 \quad \frac{d}{dx}[x] = 1 \quad \frac{d}{dx}[cx] = c$ $\frac{d}{dx}[c * f(x)] = c * f'(x)$
<b>Trigonometric Derivatives:</b>	$\frac{d}{dx}[\sin x] = \cos x \quad \frac{d}{dx}[\cos x] = -\sin x$ $\frac{d}{dx}[\tan x] = \sec^2 x \quad \frac{d}{dx}[\cot x] = -\csc^2 x$ $\frac{d}{dx}[\sec x] = \sec x \tan x \quad \frac{d}{dx}[\csc x] = -\csc x \cot x$
<b>The Power Rule:</b>	$\frac{d}{dx}[x^n] = nx^{n-1}$
<b>The Product Rule:</b>	$\frac{d}{dx}[uv] = u'v + uv'$ $\frac{d}{dx}[uvw] = u'vw + uv'w + uvw'$
<b>The Quotient Rule:</b>	$\frac{d}{dx}\left[\frac{u}{v}\right] = \frac{vu' - uv'}{v^2}$
<b>The Reciprocal Rule:</b>	$\frac{d}{dx}\left[\frac{1}{u}\right] = \frac{-u'}{u^2}$

<b>The Chain Rule:</b>	$\frac{dy}{dx} = \frac{dy}{du} * \frac{du}{dx}$ $\frac{d}{dx}[f(g(x))] = f'(g(x)) * g'(x)$ $\frac{d}{dx}[f(g(u))] = f'(g(u)) * g'(u) * u'$ $\frac{d}{dx}[f(x)]^n = n[f(x)]^{n-1} * f'(x)$
<b>Trig Derivatives:</b> “With Chain Rule”	$\frac{d}{dx} \sin(u) = \cos(u) u' \quad \frac{d}{dx} \cos(u) = -\sin(u) u'$ $\frac{d}{dx} \tan(u) = \sec^2(u) u' \quad \frac{d}{dx} \cot(u) = -\csc^2(u) u'$ $\frac{d}{dx} \sec(u) = \sec(u) \tan(u) u' \quad \frac{d}{dx} \csc(u) = -\csc(u) \cot(u) u'$
<b>Inverse Trig Derivatives:</b> “With Chain Rule”	$\frac{d}{dx} [\sin^{-1}(u)] = \frac{u'}{\sqrt{1-u^2}} \quad \frac{d}{dx} [\cos^{-1}(u)] = \frac{-u'}{\sqrt{1-u^2}}$ $\frac{d}{dx} [\tan^{-1}(u)] = \frac{u'}{1+u^2} \quad \frac{d}{dx} [\cot^{-1}(u)] = \frac{-u'}{1+u^2}$ $\frac{d}{dx} [\sec^{-1}(u)] = \frac{u'}{ u \sqrt{u^2-1}} \quad \frac{d}{dx} [\csc^{-1}(u)] = \frac{-u'}{ u \sqrt{u^2-1}}$
<b>Exponential Derivatives:</b>	$\frac{d}{dx} [e^u] = e^u * u'$ $\frac{d}{dx} [a^u] = a^u * u' * \ln a$
<b>Derivatives of Logs:</b>	$\frac{d}{dx} [\ln u] = \frac{u'}{u}$ $\frac{d}{dx} [\log_a(u)] = \frac{u'}{u \ln a}$

<b>Logarithmic Differentiation:</b>	$\frac{d}{dx} [u^v] = u^v \left[ \frac{vu'}{u} + v' \ln(u) \right]$
<b>Inverse Functions:</b>	$\frac{d}{dx} [f^{-1}(a)] = \frac{1}{f'(b)} \quad f(b) = a \quad f^{-1}(a) = b$ $\frac{d}{dx} [f^{-1}(x)] = \frac{1}{f'[f^{-1}(x)]}$
<b>Limit Definition:</b>	$f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$
<b>Alternative Definition:</b>	$f'(a) = \lim_{x \rightarrow a} \frac{f(x) - f(a)}{x - a}$